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| 4.1 | | 36 |
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| 5. | | 40 |
| 5.1. | | 41 |
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7. . . , : « », 1997. . -
8. . . .- ∴ , 2000.
9. . . . - ∴ . - ∴
10. . . . - ∴ , 1987.
11. . . . - ∴ , 2000.
12. . . , . . . - ∴ 2002
13. . . , . . , 1. . - ∴ - .2000.
14. . . .- ∴:2003.

2.

(, .).
 X,Y,Z,...,W.
 X,Y,Z,...,W - (),

- ,

« » $T\{\min(X,Y,Z,W)\}$. « »
 (« »)

$T\{\min(X,Y,Z,W)\}$

(« »)

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2.1

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(. : 1).

(X, R) , $X - A$ $R - n (-)$,
 R

- 1) $a_i \in A$ $a_i R a_i ()$;
- 2) $a_i, a_j \in A, i \neq j$ $a_i R a_j, a_j R a_i$
 $()$;
- 3) $a_i, a_k, a_j \in A$ $a_i R a_k, a_k R a_j, a_j R a_i$
 $()$.

$$a^*_i : \bigcup_i a_i^* = A.$$

2.2.

$1,$
 $R,$
 $a_i^* - (-)$
 $- 0,$

≤ 8

$S_n =$

$[6].$

$S_n:$

$$\begin{aligned}
 S_n &= 1 + \sum_{j=2}^n [n/j] + \sum_{j=2}^{n/2} \sum_{l=j+1}^{n-j} \sum_{p=1}^{[n/l]} [n-lp/j], & n > 2 \\
 &= 1 + \sum_{j=1}^n [n/j] + \sum_{j=2}^{[n/2]+1} \sum_{l=j+1}^{n-j} \sum_{p=1}^{[n/l]} [n-lp/j], & n > 2 \\
 &= [n/j] - n/j; & (n-lp) < 0, \quad [n-lp/j] = 0.
 \end{aligned}$$

[5].

$\leq 8:$

$$\begin{array}{cccccccc}
 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\
 S_n & 1 & 2 & 3 & 5 & 7 & 11 & 15 & 22
 \end{array}$$

$$\Delta^2 S_n = 0, \quad S_n < 8 -$$

$$\Delta^2 S_n = n - 2/2, \quad \leq 8 -$$

$$\Delta S_n = S_n - S_{n-1}, \quad \Delta^2 S_n = \Delta S_n - \Delta S_{n-1}.$$

$$a_i^* ()$$

« »

$C^{(n-1)}, \dots, C^{(2)}, C^{(1)}$.

$S_n - n$

$R_n = S_n - 1$

$R_n = S_n - 1$

$R_n \geq 0$.

R_n

(\dots)

= 1,2, ...7, 8:
1 2 3 4 5 6 7 8
R_n 0 0 0 1 2 5 8 14

(, -)

(- n=4).

| | | | | | |
|---|--------------|--------------|--------------|--------------|--------------|
|) | | | | | |
| | $1\ 0\ 0\ 0$ | $1\ 1\ 0\ 0$ | $1\ 1\ 0\ 0$ | $1\ 1\ 1\ 0$ | $1\ 1\ 1\ 1$ |
| | $0\ 1\ 0\ 0$ | $1\ 1\ 0\ 0$ | $1\ 1\ 0\ 0$ | $1\ 1\ 1\ 0$ | $1\ 1\ 1\ 1$ |
| | $0\ 0\ 1\ 0$ | $0\ 0\ 1\ 0$ | $0\ 0\ 1\ 1$ | $1\ 1\ 1\ 0$ | $1\ 1\ 1\ 1$ |
| | $0\ 0\ 0\ 1$ | $0\ 0\ 0\ 1$ | $0\ 0\ 1\ 1$ | $0\ 0\ 0\ 0$ | $1\ 1\ 1\ 1$ |



. 1. $n = 4$

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— (S^(k) — , k = 1,2,...,5).

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1 2 (.),

1 3 2 3 4.

(2ⁿ ,)

, S_n , $n = 8$ 0,636. = 4.
 $R_4 = S_4 - 4 = 5 - 4 = 1$.

« »
 $S^{(2)} S^{(3)}$
 $S_n R_n$ n

$S_n -$

$S_{n_1+n_2} > S_{n_1} + S_{n_2}$.

$S_{n_1+n_2} -$ $1 + 2$ [6],

2.3

R

$a_i, a_j, a_k -$, $i \neq j; i, j, k = 1, 2, \dots$

R [3].

$$(a_i, a_j) \leq (a_i/a_k) + (aj/a_k), \tag{2.1}$$

$(a_i/a_k), (aj/a_k) -$ $a_i a_j$;

$(a_i, a_j) -$
 $a_i, a_k, a_j \in A$ (
 $) a_i a_k, a_k a_j, a_i a_j$.

(1.1)

(2.1)

(2.1)

[3]:

$$(a_i/a_k) < (a_i) \quad (a_j/a_k) < (a_j),$$

H(.)

(.)

$$(a_i/a_k) + (a_j/a_k) < (a_i) + (a_j).$$

(1.1)

$$(a_i, a_j) \leq (a_i/a_k) + (a_j/a_k) < (a_i) + (a_j), \quad \dots \quad (a_i, a_j) < (a_i) + (a_j),$$

$$K = (a_i/a_k) + (a_j/a_k) - (a_i, a_j)$$

K ≥ 0,

K < 0,

; i ≠ k ≠ j; i, k, j = 1, 2, ...

(1.1).

(2.1)

... K < 0.

: 1 -

; 2 -

; 3 -

1

3,

$$(A_1 \subset A_3, A_2 \subset A_3).$$

X, Y, Z

| | | |
|--|-------------------------------|-------------------------------|
| | $X_1=1$ () ₁) | $x_2=0$ () ₁) |
| | 1/6 | 5/6 |

| | | |
|-----|-------------------------------|-------------------------------|
| Y | $Y_1=1$ () ₂) | $y_2=0$ () ₂) |
| | 1/6 | 5/6 |

| | | |
|-----|----------------|----------------|
| Z | $z_1=1$ () | $z_2=0$ () |
| | 11/36 | 25/36 |

, $P(z_1=1) = P(x_1=1 \text{ and } z_1=1) + P(x_2=1 \text{ and } z_1=1) - P(x_1=1)P(z_1=1)$
 $= 1/6 + 1/6 - 1/6 \cdot 1/6 = 11/36.$

, , Z, Z, Y -
 , $H(X,Y) > H(X/Z) + H(Y/Z), \dots < 0.$

$(X, Y) = - \sum_{j=1}^2 \sum_{i=1}^2 p(x_i, y_j) \ln p(x_i, y_j) =$
 $= - 1/36 \ln(1/36) - 5/6 \cdot 1/6 \ln(5/36) - 1/6 \cdot 5/6 \ln(5/36) - 5/6 \cdot 5/6 \ln(25/36) =$
 0.910.

$(X/Z) = - \sum_{j=1}^2 \sum_{i=1}^2 p(x_i, z_j) \ln p(x_i / z_j) =$
 $= - 1/6 \ln(6/11) - 5/6 \cdot 1/6 \ln(5/11) - 0 - 5/6 \cdot 5/6 \ln 1 = 0.206.$

$H(X/Z) = H(Y/Z).$

$H(X,Y) = 0.910; H(X/Z) + H(Y/Z) = 0.412.$

$K = - 0.412.$

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(,), (), (), ().

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« » (,) X, Y, Z W , ... X -

« » , Y - ...

f (X,Y,Z,W) -

“ ” ()

T (min {X,Y,Z,W }) .

X , Y , Z , W --

(1.1)

$$\begin{aligned}
 H(X_1, X_3) &= - \int_0^\infty \int_0^\infty f_{13}(x_1, x_3) \ln f_{13}(x_1, x_3) dx_1 dx_3 \leq \\
 &\leq H(X_1 / X_2) = - \int_0^\infty \int_0^\infty f_{12}(x_1, x_2) \ln f_{12}(x_1 / x_2) dx_1 dx_2 - \\
 &- H(X_3 / X_1) = - \int_0^\infty \int_0^\infty f_{32}(x_3, x_2) \ln f_{32}(x_3 / x_2) dx_3 dx_2 \quad (2.2)
 \end{aligned}$$

X_1, X_2, X_3
 $\{X, Y, Z, W\}$.

1, 2, 3
 :

— $f(x) = x^{n-1} [(N-1)!]^{-1} v^N \exp(-vx)$,
 N, v — ,

— $f(x) = 1/\sigma(\ln(x)) (2\pi)^{1/2} \exp(-1/2(\ln x - a(\ln x)/\sigma(\ln x))^2)$,
 $a(\ln(x))$ — $\sigma(\ln x)$ — ,

$$f_i(x_i) = 1/ek \lambda_i \exp(-\lambda_i x_i) / (1 + \lambda_i x_i), \lambda_i > 0, x_i \geq 0, \quad (2.3)$$

$$k = \int_1^\infty x_i^{-1} \exp(-x_i) dx_i, i = 1, 2, 3 \quad (2.4)$$

$$\int_0^{\infty} f(x_i) dx_i = 1 \quad \int_0^{\infty} f_{ij}(x_i, x_j) dx_j = f_i(x_i),$$

$$f_{ij}(x_i, x_j) = 1/e^k \lambda_i \lambda_j \exp(-\lambda_i x_i - \lambda_j x_j - \lambda_i \lambda_j x_i x_j) \quad (2.5)$$

(1.5)

$$f_{ij}(x_i, x_j) \neq f_i(x_i) f_j(x_j), i \neq j. \quad (2.6)$$

(1.6)

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2), (, 3) (, 4).

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(N) ,

C_N^2 (N

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$$f_i(x) = \lambda_1 \lambda_2 \lambda_3 \exp(-\lambda_1 x - \lambda_2 x - \lambda_3 x), \quad (2.2)$$

$$f_{ij}(x_i/x_j) = f_{ij}(x_i, x_j) / f_j(x_j), \quad i \neq j. \quad (2.3)$$

$$f_{ij}(x_i/x_j) = f_{ij}(x_i, x_j) / f_j(x_j), \quad i \neq j. \quad (2.4)$$

$$\ln \lambda_1 \lambda_3 \geq (1/1 - ek) (2ek_1 + \ln k + e - 1), \quad (2.7)$$

$$k_1 = \int_1^{\infty} x_i^{-1} \exp(-x_i) \ln x_i dx_i.$$

$$k_1 = 0.09783 \quad k = 0.21942 (10^{-5})$$

$$\ln(\lambda_1 \lambda_3) \geq 1.51678.$$

$$\ln(\lambda_1 \lambda_4) \geq 1.51678$$

$$\ln(\lambda_3 \lambda_4) \geq 1.51678$$

$$\ln(\lambda_1 \lambda_3) \geq 1.51678$$

$$\ln(\lambda_3 \lambda_2) \geq 1.51678$$

$$\ln(\lambda_3 \lambda_4) \geq 1.51678$$

$$\ln(\lambda_2 \lambda_4) \geq 1.51678.$$

$$\lambda_1 = \lambda_2 = \lambda_3 = \lambda_4 = 2.12.$$

$$\lambda = 2.12$$

$$T\{\min(X, Y, Z, W)\}$$

$$f(x) = (1/ek) \lambda \exp(-\lambda x) / (1 + \lambda x), \quad \lambda = 2.12.$$

$$P(t \leq T\{\min(X, Y, Z, W)\} \leq t_1) = \int_t^{t_1} f(x) dx = \int_t^{t_1} (1/ek) \lambda \exp(-\lambda x) / (1 + \lambda x) dx \quad (2.8)$$

2.4

(Z) (W). T{min(X,Y,Z,W)} - (« ») (X), (Y),

T{min (X,Y,Z,W)}.

() () .

(. .). X,Y,Z,W - (, , . .) - , , ,

T{min(X,Y,Z,W)} - « - (-) .

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$T\{\min(X, Y, Z, \dots, W)\}$ – « »

X, Y, Z, ..., W (,)

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A

$$R(A) = P(A) Y(A), \tag{2.9}$$

P(A) - A, Y (A) - A,

A,

[4]

(2.9),

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$$R^*(A) = Y(A) \tag{2.10}$$

$$(R^*) (A) = P(A) \tag{2.11}$$

(2.11) ,

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(R*)(A)
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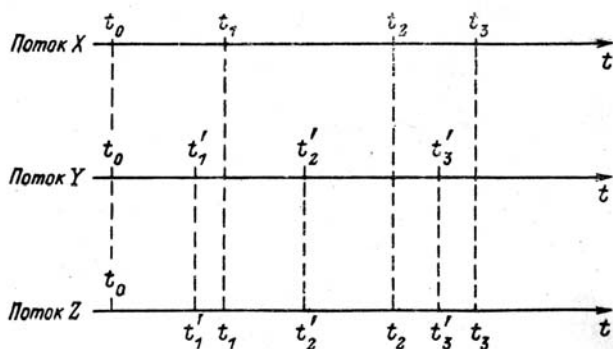
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- 1) x_1, x_2, \dots () ;
- 2) x_2, x_3, \dots ($k < t$) = $F(t)$
 $k = 2, 3, 4, \dots$
- $F_1(t) = (x_1 < t)$
 $F_1(t) \neq F(t)$.
- $F(t) = (k < t), k = 2, 3, \dots$

(1).



2. t_i, t'_i ()

1. -

$F(t) -$, $F_1(t) -$
 $F_1(t) = P(x_1 < t)$.

$\mu -$

$$F_1(t) = \frac{1}{\mu} \int_0^t (1 - F(\Theta)) d\Theta$$

Y

1, 2, 3 ..., $y_1, y_2, y_3 \dots$ $x_1, x_2, \dots -$
 X, $y_1, y_2, \dots -$ Y.
 Y - .2. Z,

(), Y.

2.

2. Y - $F_1^{(X)}$ $F_1^{(Y)}$ -

Y. $F_x \oplus F_y -$

$$(F_X \oplus F_Y)(t) = F_1^{(X)}(t) + F_1^{(Y)}(t) - F_1^{(X)}(t) F_1^{(Y)}(t)$$

Z -

$$F_Z$$

Z.

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...

$$F_{X_1} \oplus F_{X_2},$$

$$F_{X_1} \oplus F_{X_2}$$

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$$F_Z$$

$$F_{X_1} \oplus F_{X_2},$$

1 2

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H.

$$F_Z$$

$$F_{X_1} \oplus F_{X_2}$$

.

H₁:

x -

,

$$f_j(x)$$

:

$$f_j(x) = \frac{x^{N_j-1}}{(N_j-1)!} \nu_j^{N_j} \exp(-\nu_j x) \tag{2.12}$$

$$N_j = 1, 2, \dots, \nu_j > 0, j = 1, 2. \tag{2.12},$$

i = 1, 2, ..., n.

$$\chi^2.$$

i > 0

$$N^* \nu^*,$$

-

$$\chi^2.$$

1. N*, ν*.

H₁, N = N* ν = ν*,

1 II.

H₁

$$L(\underline{x}, N, \nu) = \prod_{i=1}^n f(x_i) = \frac{\prod_{i=1}^n x_i^{N-1}}{((N-1)!)^n} \nu^{nN} \exp(-\nu \sum_{i=1}^n x_i)$$

$\underline{x} = x_1, x_2, \dots, x_n.$

$\nu^* N^*$

$\nu N,$

$$L(\underline{x}, N, \nu).$$

$$r = \prod_{i=1}^n x_i; \quad s = \sum_{i=1}^n x_i; \quad g = \frac{s}{\sqrt[n]{r n}}.$$

$$S/n, \quad \sqrt[n]{r}, \quad g \geq 1; \quad g = 1$$

$$x_1 = x_2 = \dots = x_n.$$

$$N^* \quad \nu^*,$$

(3 4).

3. $\delta_k = (1 + 1/k)^{k+1}, \quad k = 1, 2, \dots$

) $g > 1 \quad \delta_1 \leq g, \quad \delta_k \leq ge \quad k = 1, 2, \dots;$

) $g > 1 \quad \delta_1 > g,$

$k_0, \quad \delta_k > ge \quad 1 \leq k < k_0 \quad \delta_j \leq g \quad j \geq k_0;$

) $g = 1, \quad \delta_k > g \quad k = 1, 2, \dots$

).

4.

1. $g > 1.$

$L(\bar{x}, N, \nu) \quad \nu^* = nN^*/S,$

) $g \geq 4, \quad N^* = 1;$

) $g < 4, \quad N^* = k_0.$

2. $g = 1,$

II.

H₁

χ^2

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(1.10) (1.11)

$Y(A) = C Y(A), \quad (2.13)$
 $CY(A) -$

, $Y(A) -$

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2. . . . 4. – 2000.- 3. – . 89-98. . 2- . .1 . – .:
3. 1999. – 258 . . 1976. – 457 .
4. . . . (. – 1993.- .3. – .16-41.
5. . . . // .-2003. 2. – .17-34.
6. – .: ,1982. – 252 .

3.

» (applied ethics).

3.1

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3.2

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$t_0 -$, $t_1 -$
 $[t_0, t_1]$ z

t_1 () z

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$t_2 -$

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t_1 ,

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t_2 z ,

(, commutivity,
 t_1).

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- t_3
 $(t_2, t_3]$

t_3 t_4

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t_4 , t_5 « » .
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 , t_5 t_6 ,
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3.3

$F(t) = z_0 \exp(-ht)$, z_0 — , h —
 , t — ,
 — , ()
 $L(t) = (a - \exp(-rt)) + b$
 t .
 r — , b — , a —
 .
 , $F(t), L(t)$ — ,

$$R(t) = F(t) - L(t).$$

t .

$R(t)$,

$$P(R(t) \geq s) = a_0,$$

P - , s, a_0 - ,

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$F(t)$ $L(t)$,

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3. , 1994, 3 - 4 .
4. « » , 2001.
5. , 1993 - . 114.
6. *Donaldson T.* The ethics of Enternational Business/ - New York, 1992. 6/ 7. Stevens Ed. Business Ethics. New York, 1979.

4.

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4.1.

$S_0,$

$X,$ $D_1(X),$
 $Y,$ $D_2(Y).$
 $R_1(X) -$ X
 $R_2(Y) -$ Y
 n ()

4.2

X_i $Y_i -$ $S_i -$ $i -$ $i -$
 $i = 1, 2, \dots, n.$

$$S_i = R_1(X_i) + R_2(Y_i),$$

$$S_{i-1} = X_i + Y_i.$$

$$S_i = R_1(X_i) + R_2(S_{i-1} - X_i).$$

$$F(X_1, X_2, \dots, X_n, Y_1, Y_2, \dots, Y_n) = \sum_{i=1}^n (D_1(X_i) + D_2(Y_i)) \rightarrow \max.$$

$$X_1 + Y_1 = S_0,$$

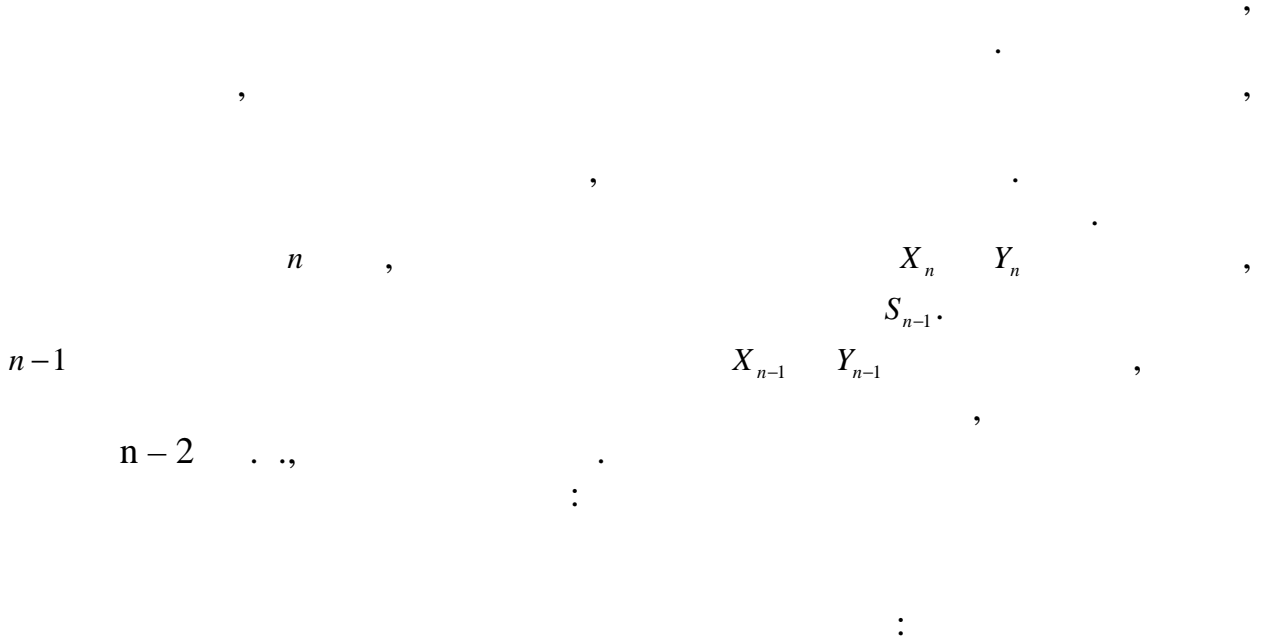
$$X_2 + Y_2 = S_1,$$

$$X_3 + Y_3 = S_2,$$

.....

$$X_n + Y_n = S_{n-1}.$$

4.3



$$D_n = \max\{D_1(X_n) + D_2(Y_n)\} = \max\{D_1(X_n) + D_2(S_{n-1} - X_n)\}$$

$$0 \leq X_n \leq S_{n-1} \quad 0 \leq X_n \leq S_{n-1}$$

$$D_{n-1,n} = \max\{D_1(X_{n-1}) + D_2(Y_{n-1}) + D_n(S_{n-1})\} = \max\{D_1(X_{n-1}) + D_2(S_{n-2} - X_{n-1}) + D_n(R_1(X_{n-1}) + R_2(S_{n-2} - X_{n-1}))\}$$

$$0 \leq X_{n-1} \leq S_{n-2} \quad 0 \leq X_{n-1} \leq S_{n-2}$$

$$S_0.$$

$$S_0=100, n=3, D_1(X) = X^2, D_1(Y) = 2Y^2, R_1(X) = 0.8X, R_2(Y) = 0.3Y.$$

$$F(X_1, X_2, X_3, Y_1, Y_2, Y_3) = \sum_{i=1}^3 (D(X_i) + D(Y_i)).$$

$$X_1 + Y_1 = 100, X_2 + Y_2 = S_1, X_3 + Y_3 = S_2.$$

$$D_3 = \max\{D_1(X_3) + D_2(Y_3)\} = \max\{D_1(X_3) + D_2(S_2 - X_3)\} =$$

$$0 \leq X_3 \leq S_2 \quad 0 \leq X_3 \leq S_2$$

$$= \max\{X_3^2 + 2(S_2 - X_3)^2\} = \max\{X_3^2 + 2(S_2^2 - 2S_2X_3 + X_3^2)\} =$$

$$0 \leq X_3 \leq S_2 \quad 0 \leq X_3 \leq S_2$$

$$= \max\{3X_3^2 + 2S_2^2 - 4S_2X_3\}.$$

$$0 \leq X_3 \leq S_2$$

$$(S_2 - \quad),$$

,

,

$$0 \leq X_3 \leq S_2.$$

$$D_3(X_3 = 0) = 2S_2^2,$$

$$D_3(X_3 = S_2) = 3S_2^2 + 2S_2^2 - 4S_2S_2 = S_2^2.$$

,

$$2S_2^2,$$

$$X_3 = 0.$$

$$Y_3 = S_2.$$

:

$$D_{2,3} = \max\{D_1(X_2) + D_2(Y_2) + D_3(S_2)\} = \max\{D_1(X_2) + D_2(S_1 - X_2) + D_3(R_1(X_2) + R_2(S_1 - X_2))\}$$

$$0 \leq X_2 \leq S_1$$

$$0 \leq X_2 \leq S_1$$

$$= \max\{X_2^2 + 2(S_1 - X_2)^2 + 2(0.8X_2^2 + 0.3(S_1 - X_2))^2\} = \max\{0.5X_2^2 - 3.45S_1X_2 + 2.18S_1^2\}.$$

$$0 \leq X_2 \leq S_1$$

$$0 \leq X_2 \leq S_1$$

$$D_{2,3}(X_3 = 0) = 2.18S_1^2,$$

$$D_{2,3}(X_3 = S_1) = 1.28S_1^2.$$

,

$$2.18S_1^2,$$

$$X_2 = 0, Y_2 = S_1.$$

:

$$D_{1,2,3} = \max\{D_1(X_1) + D_2(100 - X_1) + 2.18S_1^2\} =$$

$$0 \leq X_1 \leq S_0 = 100$$

$$= \max\{D_1(X_1) + D_2(100 - X_1) + 2.18(0.8X_1 + 0.3(100 - X_1))^2\} =$$

$$0 \leq X_1 \leq S_0 = 100$$

$$= \max\{X_1^2 + 2(100 - X_1)^2 + 2.18(0.8X_1 + 0.3(100 - X_1))^2\}.$$

$$0 \leq X_1 \leq S_0 = 100$$

$$1 \quad 2$$

$$D_{1,2,3}(X_1 = 0) = 21962,$$

$$D_{1,2,3}(X_1 = 100) = 23952.$$

,

$$23 \ 952, \quad X_1 = 100, Y_1 = 0.$$

,

$$100$$

:

1.

$$100$$

,

$$-0$$

.

2.

$$0$$

.

: $R_1(X_1 = 100) = 0.8 * 100 = 80.$

, 80

3.

0

$R_2(Y_2 = 80) = 0.3 * 80 = 24.$

24

23 952

) ((),

:
 $D_1 = 2Y^2 = 2 * 100^2 = 20000,$ $0.3 * 100 = 30,$
 $D_2 = 2 * 30^2 = 1800,$ $0.3 * 30 = 9,$
 $D_3 = 2 * 9^2 = 162.$

$20\ 000 + 18\ 00 + 162 =$

21962,

1.

2.

- ∴

. - ∴

. - 1987.

. - 1979.

/

5.

(. . .)

[4],[5],[7].

$$Z = f(\overset{\mathbf{r}}{x}), \overset{\mathbf{r}}{x} = (x_1, x_2, \dots, x_n) \quad \Omega,$$

$$f(x)$$

$$Z = f(\overset{\mathbf{l}}{x}), \overset{\mathbf{l}}{x} = (x_1, x_2, \dots, x_n)$$

$$a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n = b_1;$$

$$a_{k1}x_1 + a_{k2}x_2 + \dots + a_{kn}x_n = b_k, k \geq 0;$$

$$a_{k+1,1}x_1 + a_{k+1,2}x_2 + \dots + a_{k+1,n}x_n \leq b_{k+1};$$

(5.1)

$$a_{l1}x_1 + a_{l2}x_2 + \dots + a_{ln}x_n \leq b_l, l \geq k;$$

$$a_{l+1,1}x_1 + a_{l+1,2}x_2 + \dots + a_{l+1,n}x_n \geq b_{l+1};$$

$$a_{m1}x_1 + a_{m2}x_2 + \dots + a_{mn}x_n \geq b_m, m \geq l;$$

$$x_{j_1} \geq 0, x_{j_2} \geq 0, \dots, x_{j_p} \geq 0$$

$$Z = c_1x_1 + c_2x_2 + \dots + c_nx_n + c_0 \rightarrow \max(\min)$$

(5.2)

$$c_0, c_j, a_{ij} \in R (i=1, \dots, m, j=1, \dots, n), j_1, j_2, \dots, j_p -$$

1, 2, ... , n :

$$\{j_1, j_2, \dots, j_p\} \subset \{1, 2, \dots, n\}.$$

$$(5.1) \quad k=0 \leq m=l$$

$$l=k \geq$$

(5.1)-(5.2)

(5.1)-(5.2)
 $k=0, m=l$ (. . .) (5.1)
 $\leq), p=n$ (. . .)
 $c_0=0$ (. . .) (5.2)).

5.1.

(. . .)
 1 . . .)

1

(5.1).

5.1

| | | | |
|--|-----|------|--------|
| | 1 | | |
| | 0,4 | 0,4 | 120 |
| | 3 . | 5 . | 1500 . |
| | 0,5 | 0,25 | 100 |

1

3 . . ,

1 - 6 . .

).

Ω .

()

$x_1 -$ () ,
 $x_2 -$ () ,

: $0,4x_1 + 0,4x_2$.

120 . : $3x_1 + 5x_2$.

1500 . : $0,25x_1 + 0,5x_2$.

100

:

$$0,4x_1 + 0,4x_2 \leq 120; 3x_1 + 5x_2 \leq 1500; 0,5x_1 + 0,25x_2 \leq 100,$$

$$x_j \geq 0, j=1,2 \quad (\quad) .$$

3x₁ + 6x₂ . . . , , , . -

, Z = 3x₁ + 6x₂ → max .

5.2.

2 . -

20% , 10%, 40% , 30% : -

5.2

5.2 1 .

| | , 1 | | 1 , | .. , |
|--|------|------|------|------|
| | | | 1 , | |
| | 0,25 | 0,15 | 0,35 | 5 |
| | 0,08 | 0,04 | 0,6 | 2 |

?

: x₁ -

() , x₂ -

() .

x₁ + x₂ , 2 . , -

x₁ + x₂ ≥ 2 () , , -

0,25x₁ + 0,08x₂

0,25x₁ + 0,08x₂ ≥ 0,2(x₁ + x₂). 10%:

0,15x₁ + 0,04x₂ ≥ 0,1(x₁ + x₂), 40%: 0,15x₁ + 0,04x₂ ≤ 0,4(x₁ + x₂).

$$30\%: 0,35x_1 + 0,6x_2 \geq 0,3(x_1 + x_2).$$

$$\begin{aligned} & x_1 \quad x_2 : \\ & x_1 + x_2 \geq 2; 0,05x_1 - 0,12x_2 \geq 0; 0,05x_1 - 0,06x_2 \geq 0; 0,25x_1 + 0,36x_2 \geq 0; \\ & 0,05x_1 + 0,3x_2 \geq 0, \\ & x_j \geq 0, j = 1, 2 \end{aligned}$$

$$Z = 5x_1 + 2x_2 \rightarrow \min.$$

5.3.

| | | | | |
|--------------|---------------|-------------|---------------|--------------|
| 6:00 – 10:00 | 10:00 – 14:00 | 14:00-18:00 | 18:00 – 22:00 | 22:00 – 2:00 |
| 10 | 4 | 6 | 12 | 4 |

2:00 6:00

8

– 22:00; 22:00 – 6:00,

10

;

–

12

6:00 – 14:00; 14:00

4

$$10+12+4=26.$$

6:00, x_2 -

x_1 -

10:00, x_3 -

14:00, x_4 -

18:00, x_5 -

22:00, x_6 -

2:00.

$x_1 + x_6 \geq 10; x_1 + x_2 \geq 4; x_2 + x_3 \geq 6; x_3 + x_4 \geq 12; x_4 + x_5 \geq 4; x_5 + x_6 \geq 0,$
 $x_j \geq 0, j = 1, 2, \dots, 6$

$Z = x_1 + x_2 + x_3 + x_4 + x_5 + x_6 \rightarrow \min.$

5.4.

. 1.1.

| | | |
|--------------------|--|----------------|
| (16 ²) | | ***** ***** |
| (8 ²) | | ***** ***** |
| (0 ²) | | |
| (24 ²) | | ***** ***** |
| (8 ²) | | * * |

.5.1.

40^2 , 100 , $- 32^2$, $- 24$

$x_j, j=1,2,\dots,5$ -
 j -
 $x_1 + x_2 + 2x_4$ $2x_2 + 2x_3$ $x_1 + x_3 + 2x_5$,
 y_1, y_2, y_3 , , -

$$y_1 = x_1 + x_3 + 2x_5 - 200; y_2 = x_1 + x_2 + 2x_4 - 300; y_3 = 2x_2 + 2x_3 - 400.$$

$$16x_1 + 8x_2 + 24x_4 + 8x_5 + 40y_1 + 32y_2 + 24y_3.$$

$$x_1 + x_3 + 2x_5 - y_1 = 200; x_1 + x_2 + 2x_4 - y_2 = 300; 0x_1 + 2x_2 + 2x_3 - y_3 = 400;$$

$$x_j \geq 0, j=1,2,\dots,5; y_k \geq 0, k=1,2,3.$$

$$Z = 16x_1 + 8x_2 + 24x_4 + 8x_5 + 40y_1 + 32y_2 + 24y_3 \rightarrow \min$$

(, -).

MS Excel.

5.5.

1.

k_1 k_2 . 2 , - 1 .
 -2 1 k_1 3 k_2 ,
 k_1 500 , $k_2 - 900$.
 , ?

50 .

$$: x_1 = 200, x_2 = 120, Z_{\max} = 640.$$

2. « »

- « » « ».

5.3.

5.3

| | | | |
|-----|-----|-----|----|
| () | | | , |
| | « » | « » | |
| | 0,6 | 0,3 | 54 |
| | 0,3 | 0,2 | 48 |
| | 0,1 | 0,5 | 36 |

18 .., « » - 14 ..
 : $x_1 = 60, x_2 = 60, Z_{\max} = 1920$.

3. «McDonald's»

5.4.

5.4

| | | | |
|--|-----|-----|------|
| | | | 1 |
| | 0,6 | 0,6 | 27 |
| | 8 | 5 | 300 |
| | 40 | 65 | 2600 |
| | 15 | 0 | 450 |

20 .., -
 15 .. ?
 : $x_1 = 25, x_2 = 20, Z_{\max} = 800$.

4.

5.5.

5.5

| | | | |
|--|------|------|------|
| | 1 | 1 | , |
| | 0,50 | 0,75 | 8,25 |
| | 0,04 | 0,10 | 1,00 |
| | 0,45 | 0,25 | 5,00 |

1 600 .., 1 -
 - 1120 ..
 : $x_1 = 3,75, x_2 = 8,5, Z_{\max} = 11770$.

5.

400, 1500 900
 1:3:1
 1:5:3 –
 « »,
 « ».
 1 300 ..,
 1 – 400 ..
 : $x_1 = 250, x_2 = 150, Z_{\max} = 135000$.

6.

5.6.
 7 ..,
 1 – 10 ..
 ?

5.6

| | | | |
|--|-----|---|----|
| | | | |
| | 0,5 | 1 | 6 |
| | 1 | 1 | 8 |
| | 2 | 1 | 14 |

: $x_1 = 4, x_2 = 4, Z_{\max} = 68$.

7.

« »
 « »
 (5.7).
 1
 1 « » 10 ..,
 1 « » – 12 ..

5.7

| | | | |
|--|-----|-----|------|
| | « » | « » | , |
| | 0,3 | 0,4 | 800 |
| | 0,1 | 0,2 | 400 |
| | 0,6 | 0,4 | 1000 |

: $x_1 = 666 \frac{2}{3}, x_2 = 1500, Z_{\max} = 24666 \frac{2}{3}$.

8.

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5.8.

6 ..,

-

-5 ..

5.8

| | | | |
|--|---|---|----|
| | , | , | , |
| | 1 | 1 | 5 |
| | 3 | 2 | 12 |
| | 5 | 1 | 15 |

,

: $x_1 = 2, x_2 = 3, Z_{\max} = 27$.

9.

« »

-

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(5.9).

-

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«

-

»

1600 ..,

«

»

-1200 ..

5.9

| | | | |
|--|---|---|-----|
| | , | , | , |
| | 2 | 3 | 180 |
| | 4 | 1 | 240 |
| | 6 | 7 | 426 |

?

$: x_1 = 57, x_2 = 12, Z_{\max} = 105600.$

10.

,

10 22

1 000 .. , 100 ..

5 .. , (

 50)

 100%

4 .. , 60%

 3 .. , 10%

 5 ..

 -

 105 .. (

) 20

$: x_1 = 52, x_2 = 32, Z_{\max} = 15540.$

1. $t_p(i)$,
2. $t_p(j)$,
3. $t_p(k)$,
4. $t_p(l)$,
5. $t_p(m)$,
 \vdots

;

$t_p(j) = \max(t_p(i) + t(i, j)); (i, j) \in U_j^+$, (6.1)

$$\begin{aligned}
 U_j^+ &= \{i \in I \mid t_p(i) < t_p(j) - t(i, j)\}, \\
 t_p(I) = 0, t_p(S) = t_{kp}, \quad I, S &= \{i \in I \mid t_p(i) = 0\}, \\
 t_n(i) &= \min_{(i, j) \in U_i^-} (t_n(j) - t(i, j)), \quad (6.2)
 \end{aligned}$$

$$\begin{aligned}
 U_i^- &= \{j \in I \mid t_n(j) < t_n(i) + t(i, j)\}, \\
 S &= \{i \in I \mid t_n(i) = t_p(i)\}, \\
 R(i) &= t_n(i) - t_p(i), \quad (6.3)
 \end{aligned}$$

$$t_{p,n}(i, j) = t_p(i), \quad (i, j) \in U_j^+ \quad (6.4)$$

$$t_{p,o}(i, j) = t_p(i) + t(i, j), \quad (i, j) \in U_j^+ \quad (6.5)$$

$$t_{n,n}(i, j) = t_n(j) - t(i, j), \quad (i, j) \in U_i^- \quad (6.6)$$

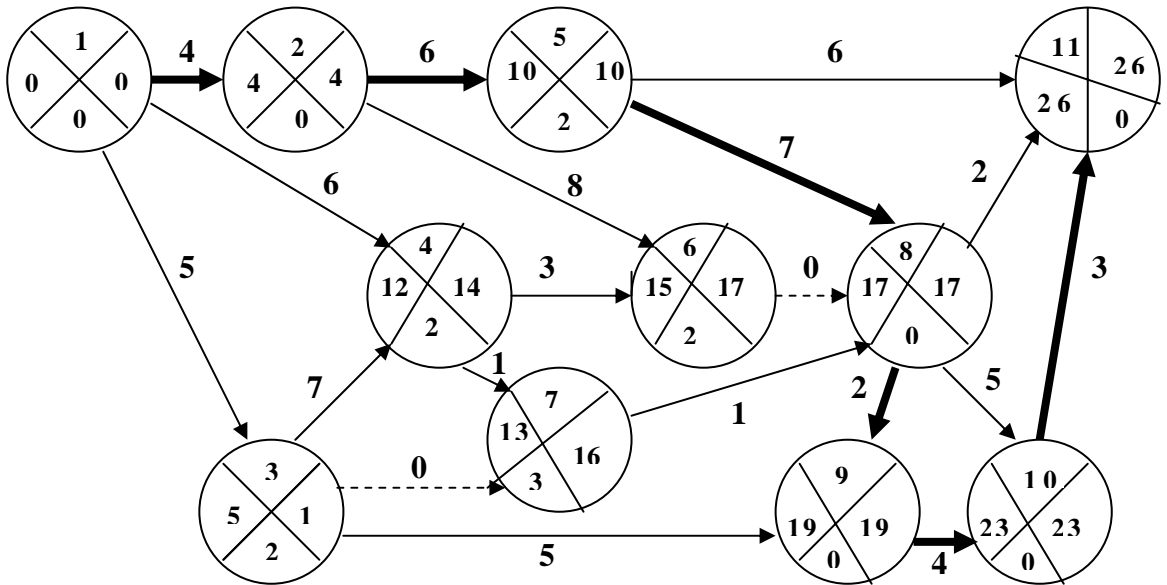
$$t_{n,o}(i, j) = t_p(j), \quad (i, j) \in U_j^+ \quad (6.7)$$

$$t_p(j) = \max_{(i, j) \in U_j^+} t_{p,o}(i, j), \quad (6.8)$$

$$t_n(i) = \min_{(i, j) \in U_i^-} t_{n,n}(i, j), \quad (6.9)$$

$$\begin{aligned}
 R_n(i, j) &= t_n(j) - t_p(i) - t(i, j) = t_n(j) - t_{p,o}(i, j) \\
 R_c(i, j) &= t_p(j) - t_p(i) - t(i, j)
 \end{aligned} \quad (6.10)$$

$$R_c(i, j) = t_p(j) - t_p(i) - t(i, j) = t_p(j) - t_{p.o}(i, j) \quad (6.11)$$



. 6.1.

() i , - i ,
 $t_p(j)$ - $R(i)$.
 $t_n(i)$ - $t_p(j), t_n(i), R(i)$

I .
 1
 $t_p(1) = 0$, 1 0.
 2, (1, 2).
 (6.1) $t_p(1) = 0$ $t(1,2) = 4$
 $t_p(2) = 4$ 2.
 $t_p(3) = t_p(1) + t(1,3) = 0 + 5 = 5$ 3.
 $t_p(4)$, 4 :
 (1, 4) (3, 4). : $t_p(1) + t(1,4)$ $t_p(3) + t(3,4)$. (6.1)

$$t_p(4) = \max(t_p(1) + t(1,4), t_p(3) + t(3,4)) = \max(0 + 6, 5 + 7) = 12,$$

$$4 \quad 12.$$

$$t_p(11) = 26, \dots$$

II

$$t_n(S) = t_p(S),$$

$$11 \quad t_p(11) = 26..$$

$$(6.2) \quad t_n(10) = t_n(11) - t(10,11) = 26 - 3 = 23.$$

$$10.$$

$$t_n(9) = t_n(10) - t(9,10) = 23 - 4 = 19.$$

$$8 \quad : (8, 9), (8, 10), (8, 11),$$

$$t_n(9) - t(8,9), t_n(10) - t(8,10) \quad t_n(11) - t(8,11). \quad (6.2)$$

$$t_n(8), \dots$$

$$t_n(8) = \min(19 - 2, 23 - 5, 26 - 2) = 17.$$

8.

$$t_n(I) = t_n(1) = 0.$$

III

$$(6.3)$$

IV

$$0,$$

$$1, 2, 5, 8, 9, 10 \quad 11,$$

$$: 1-2-5-8-9-10-11.$$

$$(\quad t_p \quad t_n \quad) \quad (6.4) - (6.11).$$

$$R_n(4,7) = 16 - 12 - 1 = 3).$$

6.2.

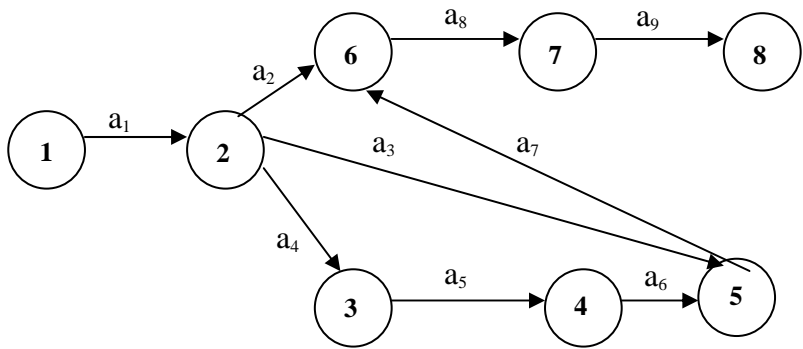
, . 6.1.

6.1

| | | |
|---------|-------|------------|
| | | |
| | a_1 | - |
| - | a_2 | a_1 |
| , , . . | a_3 | a_1 |
| | a_4 | a_1 |
| | a_5 | a_4 |
| | a_6 | a_5 |
| | a_7 | a_3, a_6 |
| , - | a_8 | a_2, a_7 |
| , | a_9 | a_8 |

a_1, a_2, \dots, a_9 .

« ».



. 6.2.

a_1 (. 6.2), , -
1, , -

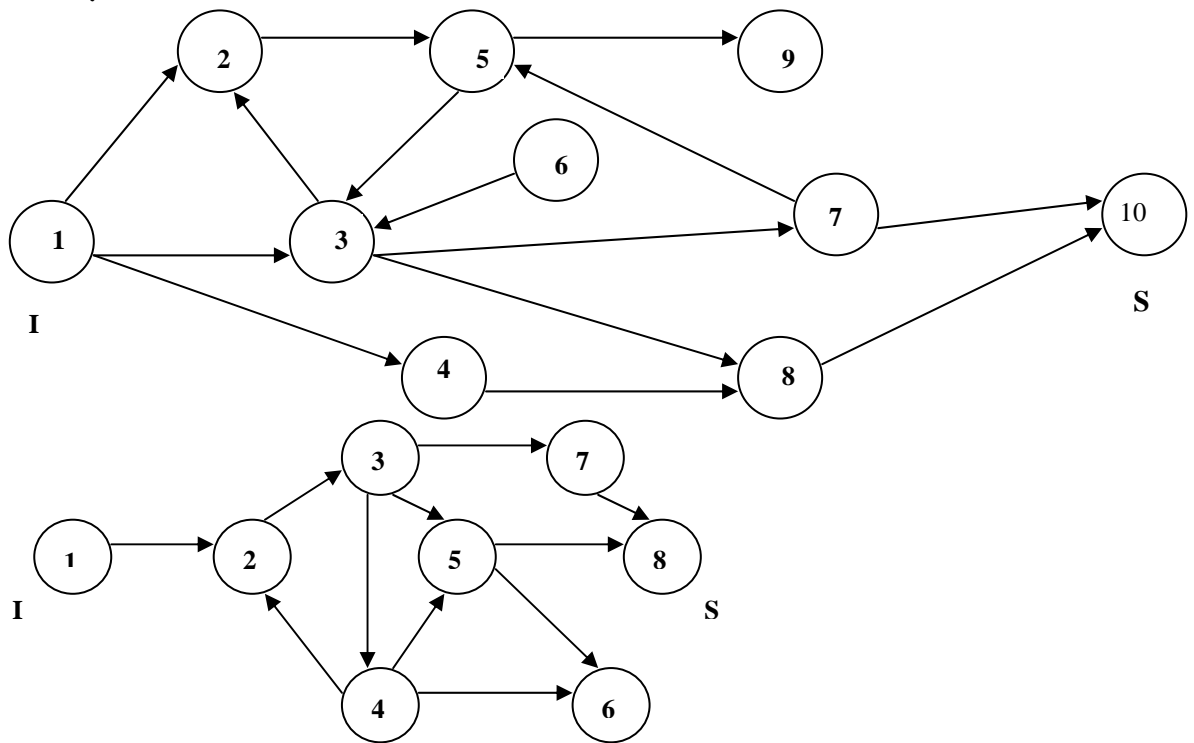
c
MS Excel.

6.3.

1.

S'

I



.6.3

2. a_2, a_3, a_4, a_5 -
 a_1, a_2, a_3, a_5 -
 a_3 .

3. $a_5, a_3, a_1, a_3, a_4, a_6, a_2$

4. $a_4, a_5, a_1, a_2, a_6, a_3, a_4, a_2$

5. $a_4, a_3, a_1, a_4, a_2, a_6, a_4, a_5, a_7$

6. $a_1, a_2, a_3, a_4, a_5, a_1, a_6, a_7, a_2, a_4, a_8, a_9, a_3, a_{10}, a_5, a_6, a_{11}, a_7, a_8, a_{12}, a_9, a_{13}, a_{10}, a_{11}, a_{12}$.

7. 6.2)

| | |
|-------|-----------------|
| | |
| a_1 | - |
| a_2 | - |
| a_3 | - |
| a_4 | a_1 |
| a_5 | a_2 |
| a_6 | a_2 |
| a_7 | a_3, a_5 |
| a_8 | a_4, a_6, a_7 |

) 6.3

| | |
|-------|-----------------|
| | |
| a_1 | — |
| a_2 | — |
| a_3 | — |
| a_4 | a_1, a_2 |
| a_5 | a_2, a_3 |
| a_6 | a_2, a_3 |
| a_7 | a_6 |
| a_8 | a_4, a_5, a_7 |

) 6.4

| | |
|-------|------------|
| | |
| a_1 | — |
| a_2 | — |
| a_3 | a_1, a_2 |
| a_4 | a_1 |
| a_5 | a_1 |
| a_6 | a_4, a_5 |
| a_7 | a_4, a_5 |
| a_8 | a_3, a_7 |

8.

6.5

| | | | |
|---|---|---|---|
| - | | - | - |
| a | | | 0 |
| b | | a | 4 |
| c | | b | 2 |
| d | , | c | 4 |
| e | | d | 6 |
| f | - | c | 1 |
| g | | f | 2 |
| h | | f | 3 |

| | | | |
|---|---|-------|----|
| i | | d | 2 |
| j | | d,g | 4 |
| k | - | i,j,h | 10 |
| l | | k | 3 |
| m | | l | 1 |
| n | - | l | 2 |
| o | | l | 3 |
| p | - | e | 2 |
| q | | p | 1 |
| r | | c | 1 |
| s | | o,t | 2 |
| t | | m,n | 3 |
| u | - | t | 1 |
| v | | q,r | 2 |
| w | - | v | 5 |
| x | | s,u,v | 0 |

9.

6.6

| | | | |
|---|---|-------|---|
| | | | , |
| 0 | | - | 3 |
| 1 | | 0 | 6 |
| 2 | | 0 | 4 |
| 3 | | 0 | 3 |
| 4 | | 1,2,3 | 1 |
| 5 | | 0 | 4 |
| 6 | | 3 | 5 |
| 7 | - | 0 | 5 |
| 8 | - | 7 | 1 |
| 9 | | 6 | 2 |

10.

15% 10% 15%

1. 1979.- 125 .
2. 2002.-116 .
3. 1995.-382
4. « », 2003. -122 .
5. 1987.- 336 .
6. 1984.- 496 .
7. 2002.-

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